

## Changing Fractions to Decimals

To change a fraction to a decimal, divide the denominator into the numerator after you put a decimal point and a few zeros to the right of the numerator. When you divide, bring the decimal point up into your answer.

*Example:* Change  $\frac{3}{4}$  to a decimal.

1. Add a decimal point and two zeros to the top number (3): 3.00
2. Divide the bottom number (4) into 3.00:  
Bring the decimal point up into the answer:  
$$\begin{array}{r} .75 \\ 4 \overline{)3.00} \\ \underline{28} \phantom{0} \\ 20 \\ \underline{20} \\ 0 \end{array}$$
3. The quotient (result of the division) is the answer: .75

Some fractions may require you to add many decimal zeros in order for the division to come out evenly. In fact, when you convert a fraction like  $\frac{2}{3}$  to a decimal, you can keep adding decimal zeros to the top number forever because the division will never come out evenly. As you divide 3 into 2, you will keep getting 6s:

$$2 \div 3 = .666666666 \text{ etc.}$$

This is called a **repeating decimal** and it can be written as  $.6\overline{6}$  or as  $.6\overline{6}\frac{2}{3}$ . You can approximate it as .67, .667, .6667, and so on.

## Changing a Fraction to a Percent and Vice Versa

To change a fraction to a percent, there are two techniques. Each is illustrated by changing the fraction  $\frac{1}{4}$  to a percent:

*Technique 1:* Multiply the fraction by 100%.  
Multiply  $\frac{1}{4}$  by 100%:  $\frac{1}{4} \times \frac{100\%}{1} = 25\%$ .

*Technique 2:* Divide the denominator into the numerator; then, move the decimal point two places to the right and tack on a percent sign (%).  
Divide 4 into 1 and move the decimal point two places to the right:

$$\begin{array}{r} .25 \\ 4 \overline{)1.00} \end{array} \quad .25 = 25\%$$

To change a percent to a fraction, remove the percent sign and write the number over 100. Then, reduce if possible.

*Example:* Change 4% to a fraction.

1. Remove the % and write the fraction 4 over 100:  $\frac{4}{100}$
2. Reduce:  $\frac{4 \div 4}{100 \div 4} = \frac{1}{25}$

*Example:* Change  $16\frac{2}{3}\%$  to a fraction.

1. Remove the % and write the fraction  $16\frac{2}{3}$  over 100:  $\frac{16\frac{2}{3}}{100}$
2. Since a fraction means “numerator divided by denominator,” rewrite the fraction as a division problem:  
 $16\frac{2}{3} \div 100$
3. Change the mixed number ( $16\frac{2}{3}$ ) to an improper fraction ( $\frac{50}{3}$ ):  $\frac{50}{3} \div \frac{100}{1}$
4. Flip the second fraction ( $\frac{100}{1}$ ) and multiply:  $\frac{50}{3} \times \frac{1}{100} = \frac{1}{6}$