

### Curve sketching and analysis

$y = f(x)$  must be continuous at each:

critical point:  $\frac{dy}{dx} = 0$  or undefined.

local minimum:  $\frac{dy}{dx}$  goes  $(-,0,+)$  or

$$(-, \text{und}, +) \text{ or } \frac{d^2y}{dx^2} > 0$$

local maximum:  $\frac{dy}{dx}$  goes  $(+,0,-)$  or

$$(+, \text{und}, -) \text{ or } \frac{d^2y}{dx^2} < 0$$

Absolute Max/Min.: Compare local extreme values to values at endpoints.

pt of inflection : concavity changes.

$$\frac{d^2y}{dx^2} \text{ goes } (+,0,-), (-,0,+), \\ (+, \text{und}, -), \text{ or } (-, \text{und}, +)$$

## Curve sketching and analysis

$y = f(x)$  must be continuous at each:

**critical point:**  $\frac{dy}{dx} = 0$  or undefined

**local minimum:** OR at endpoints

$\frac{dy}{dx}$  goes  $(-,0,+)$  or  $(-,und,+)$  or  $\frac{d^2y}{dx^2} > 0$

**local maximum:**

$\frac{dy}{dx}$  goes  $(+,0,-)$  or  $(+,und,-)$  or  $\frac{d^2y}{dx^2} < 0$

**point of inflection:** concavity changes

$\frac{d^2y}{dx^2}$  goes from  $(+,0,-)$ ,  $(-,0,+)$ ,  
 $(+,und,-)$ , or  $(-,und,+)$