

Derivative Rules:

$\frac{d}{dx}(c) = 0$	$\frac{d}{dx}(x^n) = nx^{n-1}$	
$\frac{d}{dx}(\sin x) = \cos x$ $\frac{d}{dx}(\sec x) = \sec x \tan x$ $\frac{d}{dx}(\tan x) = \sec^2 x$	$\frac{d}{dx}(\cos x) = -\sin x$ $\frac{d}{dx}(\csc x) = -\csc x \cot x$ $\frac{d}{dx}(\cot x) = -\csc^2 x$	$\frac{d}{dx}(a^x) = a^x \ln a$ $\frac{d}{dx}(e^x) = e^x$
$\frac{d}{dx}(cf(x)) = c \frac{d}{dx}(f(x))$	$\frac{d}{dx}(f(x) \pm g(x)) = \frac{d}{dx}(f(x)) \pm \frac{d}{dx}(g(x))$	
$(f \cdot g)' = f' \cdot g + f \cdot g'$	$\left(\frac{f}{g}\right)' = \frac{f'g - fg'}{g^2}$	$\frac{d}{dx}(f(g(x))) = f'(g(x))g'(x)$

Derivatives	
Definition of a Derivative of a Function Slope Function	$f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$ $f'(c) = \lim_{x \rightarrow c} \frac{f(x) - f(c)}{x - c}$
Notation for Derivatives	$f'(x), f^{(n)}(x), \frac{dy}{dx}, y', \frac{d}{dx}[f(x)], D_x[y]$
0. The Chain Rule	$\frac{d}{dx}[f(g(x))] = f'(g(x))g'(x)$ $\frac{dy}{dx} = \frac{dy}{dt} \cdot \frac{dt}{dx}$
1. The Constant Multiple Rule	$\frac{d}{dx}[cf(x)] = cf'(x)$
2. The Sum and Difference Rule	$\frac{d}{dx}[f(x) \pm g(x)] = f'(x) \pm g'(x)$
3. The Product Rule	$\frac{d}{dx}[fg] = fg' + gf'$
4. The Quotient Rule	$\frac{d}{dx}\left[\frac{f}{g}\right] = \frac{gf' - fg'}{g^2}$
5. The Constant Rule	$\frac{d}{dx}[c] = 0$
6a. The Power Rule	$\frac{d}{dx}[x^n] = nx^{n-1}$
6b. The General Power Rule	$\frac{d}{dx}[u^n] = nu^{n-1} u' \text{ where } u = u(x)$
7. The Power Rule for x	$\frac{d}{dx}[x] = 1 \text{ (think } x = x^1 \text{ and } x^0 = 1)$

Derivatives

$$\frac{d}{dx} x^n = nx^{n-1}$$

$$\frac{d}{dx} \ln x = \frac{1}{x}$$

$$\frac{d}{dx} \log_b x = \frac{1}{x \ln b}$$

$$\frac{d}{dx} e^x = e^x$$

$$\frac{d}{dx} b^x = b^x \cdot \ln b$$

$$\frac{d}{dx} \sin x = \cos x$$

$$\frac{d}{dx} \cos x = -\sin x$$

$$\frac{d}{dx} \tan x = \sec^2 x$$

$$\frac{d}{dx} \sec x = \sec x \cdot \tan x$$

$$\frac{d}{dx} \arcsin x = \frac{1}{\sqrt{1-x^2}}$$

$$\frac{d}{dx} \arccos x = -\frac{1}{\sqrt{1-x^2}}$$

$$\frac{d}{dx} \arctan x = \frac{1}{1+x^2}$$

Differentiation Formulas

$$1. \frac{d}{dx}(x^n) = nx^{n-1}$$

$$2. \frac{d}{dx}(fg) = fg' + gf'$$

$$3. \frac{d}{dx}\left(\frac{f}{g}\right) = \frac{gf' - fg'}{g^2}$$

$$4. \frac{d}{dx}f(g(x)) = f'(g(x))g'(x)$$

$$5. \frac{d}{dx}(\sin x) = \cos x$$

$$6. \frac{d}{dx}(\cos x) = -\sin x$$

$$7. \frac{d}{dx}(\tan x) = \sec^2 x$$

$$8. \frac{d}{dx}(\cot x) = -\csc^2 x$$

$$9. \frac{d}{dx}(\sec x) = \sec x \tan x$$

$$10. \frac{d}{dx}(\csc x) = -\csc x \cot x$$

$$11. \frac{d}{dx}(e^x) = e^x$$

$$12. \frac{d}{dx}(a^x) = a^x \ln a$$

$$13. \frac{d}{dx}(\ln x) = \frac{1}{x}$$

$$14. \frac{d}{dx}(\text{Arc sin } x) = \frac{1}{\sqrt{1-x^2}}$$

$$15. \frac{d}{dx}(\text{Arc tan } x) = \frac{1}{1+x^2}$$

$$16. \frac{d}{dx}(\text{Arc sec } x) = \frac{1}{|x| \sqrt{x^2-1}}$$

$$17. \frac{dy}{dx} = \frac{dy}{du} \times \frac{du}{dx} \quad \text{Chain Rule}$$

Differentiation Formulas

- $\frac{d}{dx}(x^n) = nx^{n-1}$
- $\frac{d}{dx}(fg) = fg' + gf'$ *Product rule*
- $\frac{d}{dx}\left(\frac{f}{g}\right) = \frac{gf' - fg'}{g^2}$ *Quotient rule*
- $\frac{d}{dx}f(g(x)) = f'(g(x))g'(x)$ *Chain rule*
- $\frac{d}{dx}(\sin x) = \cos x$
- $\frac{d}{dx}(\cos x) = -\sin x$
- $\frac{d}{dx}(\tan x) = \sec^2 x$
- $\frac{d}{dx}(\cot x) = -\csc^2 x$
- $\frac{d}{dx}(\sec x) = \sec x \tan x$
- $\frac{d}{dx}(\csc x) = -\csc x \cot x$
- $\frac{d}{dx}(e^x) = e^x$
- $\frac{d}{dx}(a^x) = a^x \ln a$
- $\frac{d}{dx}(\ln x) = \frac{1}{x}$
- $\frac{d}{dx}(\text{Arc sin } x) = \frac{1}{\sqrt{1-x^2}}$
- $\frac{d}{dx}(\text{Arc tan } x) = \frac{1}{1+x^2}$
- $\frac{d}{dx}(\text{Arc sec } x) = \frac{1}{|x|\sqrt{x^2-1}}$
- $\frac{d}{dx}[c] = 0$
- $\frac{d}{dx}[cf(x)] = cf'(x)$

Differentiation Rules

Prod.

$$\frac{d}{dx}(f \cdot g) = f'g + fg'$$

Quot.

$$\frac{d}{dx}\left(\frac{f}{g}\right) = \frac{f'g - fg'}{g^2}$$

Chain

$$\frac{d}{dx}f(g(x)) = f'(g(x)) \cdot g'(x)$$