

### Integration by Parts:

Knowing which function to call  $u$  and which to call  $dv$  takes some practice. Here is a general guide:

u	Inverse Trig Function	( $\sin^{-1} x, \arccos x, \text{etc}$ )
↑	Logarithmic Functions	( $\log 3x, \ln(x+1), \text{etc}$ )
↕	Algebraic Functions	( $x^3, x+5, 1/x, \text{etc}$ )
↓	Trig Functions	( $\sin(5x), \tan(x), \text{etc}$ )
dv	Exponential Functions	( $e^{3x}, 5^{3x}, \text{etc}$ )

Functions that appear at the top of the list are more like to be  $u$ , functions at the bottom of the list are more like to be  $dv$ .

### Integration By “Parts”

If  $u = f(x)$  and  $v = g(x)$  and if  $f'(x)$  and  $g'(x)$  are continuous, then

$$\int u \, dx = uv - \int v \, du .$$

Note: The goal of the procedure is to choose  $u$  and  $dv$  so that  $\int v \, du$  is easier to solve than the original problem.

### Suggestion:

When “choosing”  $u$ , remember **L.I.A.T.E.**, where **L** is the logarithmic function, **I** is an inverse trigonometric function, **A** is an algebraic function, **T** is a trigonometric function, and **E** is the exponential function. Just choose  $u$  as the first expression in **L.I.A.T.E** (and  $dv$  will be the remaining part of the integrand). For example, when integrating  $\int x \ln x \, dx$ , choose  $u = \ln x$  since **L** comes first in **L.I.A.T.E**, and  $dv = x \, dx$ . When integrating  $\int x e^x \, dx$ , choose  $u = x$ , since **x** is an algebraic function, and **A** comes before **E** in **L.I.A.T.E**, and  $dv = e^x \, dx$ . One more example, when integrating  $\int x \text{Arc tan}(x) \, dx$ , let  $u = \text{Arc tan}(x)$ , since **I** comes before **A** in **L.I.A.T.E**, and  $dv = x \, dx$ .