

## ALTERNATING SERIES

Does  $a_n = (-1)^n b_n$  or  
 $a_n = (-1)^{n-1} b_n, b_n \geq 0$ ?

— YES

Is  $b_{n+1} \leq b_n$  &  $\lim_{n \rightarrow \infty} b_n = 0$ ?

— YES →

$\sum a_n$  Converges

Alternating Series: Let  $\sum_{n=1}^{\infty} a_n$  be a series such that

- i) the series is alternating
- ii)  $|a_{n+1}| \leq |a_n|$  for all  $n$ , and
- iii)  $\lim_{n \rightarrow \infty} a_n = 0$

Then the series *converges*.

Alternating Series Remainder: The remainder  $R_N$  is less than (or equal to) the first neglected term

$$|R_N| \leq a_{N+1}$$

**Alt. Series Error:** error  $\leq |a_{n+1}|$  (the next term)