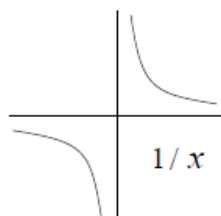


## Continuity Facts ... Set 3

We say a function is **continuous** if its *domain is an interval*, and it is continuous at every point of that interval.

A **point of discontinuity** is always understood to be isolated, i.e., it is the only bad point for the function on some interval.



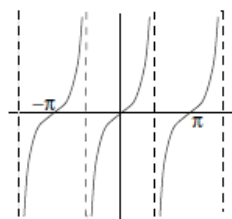
The function  $1/x$  is continuous on  $(0, \infty)$  and on  $(-\infty, 0)$ , i.e., for  $x > 0$  and for  $x < 0$ , in other words, at every point in its domain. However, it is not a continuous function since its domain is not an interval. It has a single point of discontinuity, namely  $x = 0$ , and it has an infinite discontinuity there.

## Continuity Facts ... Set 3

We say a function is **continuous** if its *domain is an interval*, and it is continuous at every point of that interval.

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We illustrate the point of these definitions. (They are slightly different from the ones in your book, but are more consistent with standard terminology in calculus.)



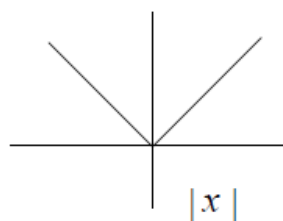
The function  $\tan x$  is not continuous, but is continuous on for example the interval  $-\pi/2 < x < \pi/2$ . It has infinitely many points of discontinuity, at  $\pm\pi/2, \pm3\pi/2$ , etc.; all are infinite discontinuities.

## Continuity Facts ... Set 3

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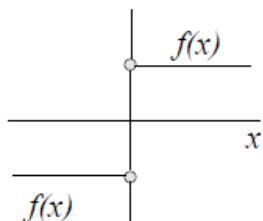
$f(x) = |x|$  is continuous.

## Continuity Facts ... Set 3

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$$f(x) = \begin{cases} 1, & x > 0, \\ -1, & x < 0 \end{cases}$$

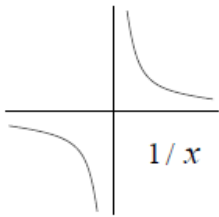
$f(x)$  discontinuous at 0.

## Continuity Facts ... Set 3

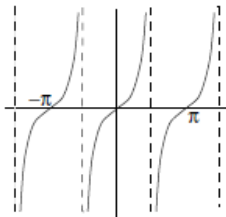
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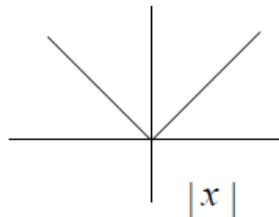
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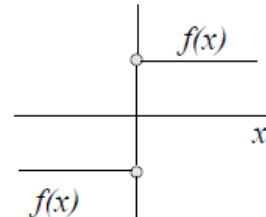
Example



Example



Example



Example