Algebraic Limits Worksheet

Given $\lim_{x \to a} f(x) = -3$, $\lim_{x \to a} g(x) = 0$, and $\lim_{x \to a} h(x) = 8$, find each limit if it exists.

1.
$$\lim_{x \to a} [f(x) + h(x)]$$
 2. $\lim_{x \to a} [f(x)]^2$

$$\lim_{x\to a} [f(x)]^2$$

3.
$$\lim_{x \to a} \sqrt[3]{h(x)}$$

4.
$$\lim_{x \to a} \frac{1}{f(x)}$$

5.
$$\lim_{x \to a} \frac{g(x)}{h(x)}$$

6.
$$\lim_{x \to a} \frac{h(x)}{g(x)}$$

7.
$$\lim_{x \to a} \frac{2f(x)}{h(x) - f(x)}$$

8.
$$\lim_{x \to a} [f(x)h(x)]$$

9.
$$\lim_{x \to a} \left[\frac{g(x) + h(x)}{f(x)} \right]$$

Evaluate the limits:

10.
$$\lim_{x \to 0} \frac{x^2 + 7x + 6}{x + 3}$$

11.
$$\lim_{x \to 2} \frac{\frac{2}{x^2} - \frac{1}{2}}{x - 2}$$

12.
$$\lim_{x \to 2} \frac{(2x+1)^2 - 25}{x-2}$$

13.
$$\lim_{h \to 0} \frac{(2+h)^3 - 8}{h}$$

14.
$$\lim_{x \to 3} \frac{x^2 - 9}{x + 3}$$

15.
$$\lim_{h \to 0} \frac{(1+h)^2 - 1^2}{h}$$

16.
$$\lim_{h \to 0} \frac{(-5+h)^2 - 25}{h}$$
 17.
$$\lim_{t \to 2} \frac{t^2 - 4}{t^3 - 8}$$

17.
$$\lim_{t \to 2} \frac{t^2 - 4}{t^3 - 8}$$

18.
$$\lim_{u \to 2} \frac{\sqrt{4u+1} - 3}{u - 2}$$

19.
$$\lim_{x \to 3} \frac{\frac{1}{x} - \frac{1}{3}}{x - 3}$$

20.
$$\lim_{h \to 0} \frac{\frac{1}{2+h} - \frac{1}{2}}{h}$$

21.
$$\lim_{x \to 2} \frac{x^4 - 2x^2 - 8}{x^2 - x - 6}$$

22.
$$\lim_{x \to -2} \frac{\frac{x}{x+4} + 1}{x+2}$$

23.
$$\lim_{x \to 3} \frac{x^2 - 9}{2x^2 + 7x + 3}$$
 24.
$$\lim_{x \to 1} \frac{x^2 - x - 2}{x - 2}$$

24.
$$\lim_{x \to 1} \frac{x^2 - x - 2}{x - 2}$$

25.
$$\lim_{x \to 1} \frac{4x^4 - 5x^2 + 1}{x^2 + 2x - 3}$$
 26.
$$\lim_{x \to 4} \frac{x^2 - 4x}{x^2 - 3x - 4}$$

26.
$$\lim_{x \to 4} \frac{x^2 - 4x}{x^2 - 3x - 4}$$

27.
$$\lim_{h \to 0} \frac{(3+h)^2 - 9}{h}$$

28.
$$\lim_{h \to 0} \frac{\frac{1}{(h+2)^2} - \frac{1}{4}}{h}$$

29.
$$\lim_{x \to 1} \frac{x^2 - 3x + 2}{x^3 - 1}$$
 30.
$$\lim_{x \to 16} \frac{4 - \sqrt{x}}{16x - x^2}$$

30.
$$\lim_{x \to 16} \frac{4 - \sqrt{x}}{16x - x^2}$$

$$\lim_{x \to 4} \frac{\sqrt{x} - 2}{x - 4}$$

32.
$$\lim_{x \to 3} \frac{3(x+1)^{-1} - 3(4)^{-1}}{x-3}$$
 33.
$$\lim_{t \to 0} \frac{\sqrt{t^2 + 9} - 3}{t^2}$$

33.
$$\lim_{t \to 0} \frac{\sqrt{t^2 + 9} - 3}{t^2}$$

34.
$$\lim_{x \to 1} \frac{\frac{2x}{x+1} - 1}{x - 1}$$

35.
$$\lim_{x \to 2} \frac{x^3 + x^2 - 4x - 4}{x^2 + x - 6}$$
 36.
$$\lim_{h \to 0} \frac{(x+h)^2 - x^2}{h}$$

36.
$$\lim_{h \to 0} \frac{(x+h)^2 - x^2}{h}$$

37.
$$\lim_{t \to -3} \frac{t^2 - 9}{2t^2 + 7t + 3}$$

37.
$$\lim_{t \to 3} \frac{t^2 - 9}{2t^2 + 7t + 3}$$
 38.
$$\lim_{x \to 0} \frac{\frac{3}{x + 5} - \frac{3}{5}}{x}$$

39.
$$\lim_{h \to 0} \frac{(3+h)^3 - 27}{h}$$

40.
$$\lim_{p \to -2} \frac{(p+4)^{-1} - 2^{-1}}{p+2}$$
 41.
$$\lim_{t \to 0} \frac{\sqrt{1+t} - \sqrt{1-t}}{t}$$
 42.
$$\lim_{x \to 3} \frac{\sqrt{x+6} - x}{x^3 - 3x^2}$$

41.
$$\lim_{t \to 0} \frac{\sqrt{1+t} - \sqrt{1-t}}{t}$$

42.
$$\lim_{x \to 3} \frac{\sqrt{x+6} - x}{x^3 - 3x^2}$$