#### Power Rule for Derivatives Practice

Differentiate each function with respect to the given variable.

1) 
$$h(r) = 2$$

2) 
$$y = -3$$

3) 
$$h(r) = -4r^4$$

4) 
$$g(t) = 2t^3$$

5) 
$$f = -\frac{1}{t^2}$$

6) 
$$f = -2x^{-3}$$

7) 
$$g = \frac{4}{x^4}$$

8) 
$$f = 4s^{-4}$$

9) 
$$g(x) = \frac{4}{x^2}$$

10) 
$$h(t) = 3t^{\frac{1}{5}}$$

11) 
$$g(s) = \sqrt[5]{s}$$

12) 
$$g(w) = 5\sqrt[5]{w^2}$$

13) 
$$f(w) = 2\sqrt[4]{w}$$

14) 
$$h = \sqrt[4]{r}$$

15) 
$$s = 4\sqrt[4]{r}$$

16) 
$$h(r) = 5\sqrt[5]{r}$$

$$17) \ h(t) = -4t^a$$

18) 
$$g(w) = 3w^{4b}$$

Answers

1) h'(r) = 0

2)  $\frac{dy}{dt} = 0$ 

3)  $h'(r) = -16r^3$  4)  $g'(t) = 6t^2$ 

5)  $\frac{df}{dt} = 2t^{-3}$  6)  $\frac{df}{dx} = 6x^{-4}$  7)  $\frac{dg}{dx} = -16x^{-5}$  8)  $\frac{df}{ds} = -16s^{-5}$ 

9)  $g'(x) = -8x^{-3}$ 

10)  $h'(t) = \frac{3}{5}t^{-\frac{4}{5}}$  11)  $g'(s) = \frac{1}{5}s^{-\frac{4}{5}}$  12)  $g'(w) = 2w^{-\frac{3}{5}}$ 

13)  $f'(w) = \frac{1}{2}w^{-\frac{3}{4}}$  14)  $\frac{dh}{dr} = \frac{1}{4}r^{-\frac{3}{4}}$  15)  $\frac{ds}{dr} = r^{-\frac{3}{4}}$  16)  $h'(r) = r^{-\frac{4}{5}}$ 

17)  $h'(t) = -4at^{a-1}$ 

18)  $g'(w) = 12bw^{4b-1}$ 

For each problem, find the instantaneous rate of change of the function at the given value.

19) 
$$y = x^2 + 2x - 2$$
; -1

20) 
$$y = -2x^2 + 2$$
;  $-1$ 

21) 
$$y = 2x^2 - 1$$
; 1

22) 
$$y = x^2 + 2x + 1$$
;  $-2$ 

For each problem, find the equation of the tangent line to the function at the given point.

23) 
$$y = x^2 - 1$$
; (2, 3)

24) 
$$v = x^2 + x + 2$$
;  $(-1, 2)$ 

25) 
$$y = x^2 + x + 1$$
; (-2, 3)

26) 
$$y = x^2 + 1$$
; (0, 1)

Evaluate each limit.

27) 
$$\lim_{h \to 0} \frac{\left(\frac{2}{3} + h\right)^2 - \left(\frac{2}{3}\right)^2}{h}$$

28) 
$$\lim_{h \to 0} \frac{\left(\frac{5}{3} + h\right)^2 - \left(\frac{5}{3}\right)^2}{h}$$

29) 
$$\lim_{t \to 0} \frac{\left(\frac{1}{3} + t\right)^4 - \left(\frac{1}{3}\right)^4}{t}$$

30) 
$$\lim_{t \to 0} \frac{\left(\frac{2}{3} + t\right)^2 - \left(\frac{2}{3}\right)^2}{t}$$

31) 
$$\lim_{x \to 0} \frac{\sqrt[3]{5+x} - \sqrt[3]{5}}{x}$$

32) 
$$\lim_{x \to 0} \frac{\left(-\frac{1}{3} + x\right)^3 - \left(-\frac{1}{3}\right)^3}{x}$$

**Answers** 

19) 0

20) 4

21) 4

22) -2

23) y = 4x - 5

24) y = -x + 1

25) y = -3x - 3

26) y = 1

27)  $\frac{4}{3}$ 

28)  $\frac{10}{3}$ 

29)  $\frac{4}{27}$ 

30)  $\frac{4}{3}$ 

31)  $\frac{\sqrt[3]{5}}{15}$ 

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