Definition of Derivative Practice Worksheet

1) Use the Limit Definition of a derivative to find f'(x) if $f(x) = 2x^2 - 3x + 1$

$$f'(x) = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h}$$

2) Use the Alternative definition of the derivative to find f'(2) if $f(x) = \sqrt{2-x}$ $f'(c) = \lim_{x \to c} \frac{f(x) - f(c)}{x - c}$

3) Use the Limit Definition of a Derivative to find f'(x) if $f(x) = \sqrt{2x-1}$

Answers

Definition of Derivative Practice Worksheet

1) Use the Limit Definition of a derivative to find f'(x) if $f(x) = 2x^2 - 3x + 1$

$$f'(x) = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h} \qquad f(x) = 2(x)^{2} - 3(x) + 1$$

$$f'(x) = \lim_{h \to 0} \frac{2(x+h)^{2} - 3(x+h) + 1 - (2x^{2} - 3x + 1)}{h} \qquad f'(x) = \lim_{h \to 0} \frac{4x + 2h^{2} - 3h}{h}$$

$$f'(x) = \lim_{h \to 0} \frac{2(x^{2} + 2x + h + 2h^{2} - 3x - 3h + 1 - 2x^{2} + 3x - 1)}{h} \qquad f'(x) = \lim_{h \to 0} \frac{h(4x + 2h - 3)}{h} = 4x + 2(0) - 3$$

$$f'(x) = \lim_{h \to 0} \frac{2x^{2} + 4x + 2h^{2} - 3x - 3h + 1 - 2x^{2} + 3x - 1}{h} \qquad f'(x) = 4x - 3$$

$$f'(x) = \lim_{h \to 0} \frac{4xh + 2h^2 - 3h}{h}$$

$$f'(x) = \lim_{h \to 0} \frac{h(4x + 2h - 3)}{K} = 4x + 2(0) - 3$$

$$f'(x) = 4x - 3$$

2) Use the Alternative definition of the derivative to find H'(2) if $H(x) = \sqrt{3-x}$

$$f'(\underline{c}) = \lim_{x \to \underline{c}} \frac{f(x) - f(\underline{c})}{x - \underline{c}}$$

$$h'(2) = \lim_{x \to 2} \frac{h(x) - h(2)}{x - 2}$$

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$$h'(2) = \lim_{x \to 2} \frac{3 - x - 1}{(x - 2)(\sqrt{3} - x + 1)}$$

$$h'(2) = \lim_{x \to 2} \frac{3 - x - 1}{(x - 2)(\sqrt{3} - x + 1)}$$

$$h(2) = \lim_{x \to 2} \frac{\sqrt{3-x} - 1}{x-2}$$

$$h'(2) = \lim_{x \to 2} (\sqrt{3-x-1})(\sqrt{3-x+1}) h'(2) = \frac{-1}{\sqrt{3-2}+1} = \frac{-1}{1+1} = \frac{-1}{2}$$

$$f'(x) = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h}$$

$$f() = \sqrt{2()-1} f(x) = \lim_{h \to 0} \frac{2x+2h-1-(2x-1)}{h[\sqrt{2x+2h-1}+\sqrt{2x-1}]}$$

$$f(x) = \lim_{h \to 0} \frac{\int 2x + 2h - 1 - \sqrt{2x - 1}}{h} \frac{\left(\sqrt{2x + 2h - 1} + \sqrt{2x - 1}\right)}{\sqrt{2x + 2h - 1} + \sqrt{2x - 1}}$$

$$f'(x) = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h}$$

4) Use the Limit Definition of a derivative to find f'(3) if $f(x) = \frac{2}{5-x}$

5) Use either general or alternative method above to find the equation of the tangent line to $f(x) = 2x - 3x^2$ at x = -1. $y - y_1 = m(x - x_1)$

Answers

$$f'(x) = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h}$$
4) Use the Limit Definition of a derivative to find $f'(3)$ if $f(x) = \frac{2}{5-x}$

$$f'(x) = \lim_{h \to 0} \frac{2}{5-(x+h)} - \frac{2}{5-x}$$

$$f'(x) = \lim_{h \to 0} \frac{2}{5-(x$$