

Calculus on a Variety of Functions ... (set 3)

Limits

Question 1: Find $\lim_{x \rightarrow 3} f(x)$:

$$f(x) = \frac{x^2 - 9}{x - 3}$$

- (A) $+\infty$
- (B) -6
- (C) 6
- (D) Does not exist!
- (E) None of the above

Calculus on a Variety of Functions ... (set 3)

Limits

Answer

Question 1: Find $\lim_{x \rightarrow 3} f(x)$:

$$f(x) = \frac{x^2 - 9}{x - 3}$$

- (A) $+\infty$
- (B) -6
- (C) 6
- (D) Does not exist!
- (E) None of the above

Answer: (C) Note the the function $f(x) = \frac{x^2-9}{x-3} = \frac{(x-3)(x+3)}{x-3} = x + 3$ is actually a line. However it is important to note the this function is *undefined* at $x = 3$. Why? $x = 3$ requires dividing by zero (which is inadmissible). As x approaches 3 from below and from above, the value of the function $f(x)$ approaches $f(3) = 6$. Thus the limit $\lim_{x \rightarrow 3} f(x) = 6$.

Calculus on a Variety of Functions ... (set 3)

Limits

Question 2: Find $\lim_{x \rightarrow 2} f(x)$:

$$f(x) = 1776$$

- (A) $+\infty$
- (B) 1770
- (C) $-\infty$
- (D) Does not exist!
- (E) None of the above

Calculus on a Variety of Functions ... (set 3)

Limits

Answer

Question 2: Find $\lim_{x \rightarrow 2} f(x)$:

$$f(x) = 1776$$

- (A) $+\infty$
- (B) 1770
- (C) $-\infty$
- (D) Does not exist!
- (E) None of the above

Answer: (E) The limit of any constant function at any point, say $f(x) = C$, where C is an arbitrary constant, is simply C . Thus the correct answer is $\lim_{x \rightarrow 2} f(x) = 1776$.

Calculus on a Variety of Functions ... (set 3)

Limits

Question 3: Find $\lim_{x \rightarrow 4} f(x)$:

$$f(x) = ax^2 + bx + c$$

- (A) $+\infty$
- (B) $16a + 4b + c$
- (C) $-\infty$
- (D) Does not exist!
- (E) None of the above

Calculus on a Variety of Functions ... (set 3)

Limits

Answer

Question 3: Find $\lim_{x \rightarrow 4} f(x)$:

$$f(x) = ax^2 + bx + c$$

- (A) $+\infty$
- (B) $16a + 4b + c$
- (C) $-\infty$
- (D) Does not exist!
- (E) None of the above

Answer: (B) Applying the rules of limits:

$$\begin{aligned}\lim_{x \rightarrow 4} ax^2 + bx + c &= \lim_{x \rightarrow 4} ax^2 + \lim_{x \rightarrow 4} bx + \lim_{x \rightarrow 4} c \\ &= a [\lim_{x \rightarrow 4} x]^2 + b \lim_{x \rightarrow 4} x + c \\ &= 16a + 4b + c\end{aligned}$$

Calculus on a Variety of Functions ... (set 3)

Limits

Question 4: Find $\lim_{x \rightarrow 8} f(x)$:

$$f(x) = \frac{x^2 + 7x - 120}{x - 7}$$

Calculus on a Variety of Functions ... (set 3)

Limits

Answer

Question 4: Find $\lim_{x \rightarrow 8} f(x)$:

$$f(x) = \frac{x^2 + 7x - 120}{x - 7}$$

Answer: Applying the rules of limits:

$$\begin{aligned} \lim_{x \rightarrow 8} \frac{x^2 + 7x - 120}{x - 7} &= \frac{8^2 + 7 * 8 - 120}{8 - 7} \\ &= \frac{120 - 120}{1} &&= \frac{0}{1} \\ &= 0 \end{aligned}$$

Calculus on a Variety of Functions ... (set 3)

Limits

Question 5: Find $\lim_{x \rightarrow 2} f(x)$:

$$f(x) = \frac{3x^2 - 4x + 6}{x^2 + 8x - 15}$$

Calculus on a Variety of Functions ... (set 3)

Limits

Answer

Question 5: Find $\lim_{x \rightarrow 2} f(x)$:

$$f(x) = \frac{3x^2 - 4x + 6}{x^2 + 8x - 15}$$

Answer: Applying the rules of limits:

$$\begin{aligned} \lim_{x \rightarrow 2} \frac{3x^2 - 4x + 6}{x^2 + 8x - 15} &= \frac{3(2)^2 - 4(2) + 6}{(2)^2 + 8(2) - 15} \\ &= \frac{12 - 8 + 6}{4 + 1} &&= \frac{10}{5} \\ &= 2 \end{aligned}$$

Calculus on a Variety of Functions ... (set 3)

Limits

Question 6: Find $\lim_{x \rightarrow \infty} f(x)$:

$$f(x) = \frac{9}{4x^2 - 7}$$

Calculus on a Variety of Functions ... (set 3)

Limits

Answer

Question 6: Find $\lim_{x \rightarrow \infty} f(x)$:

$$f(x) = \frac{9}{4x^2 - 7}$$

Answer: Applying the rules of limits:

$$\begin{aligned} \lim_{x \rightarrow \infty} \frac{9}{4x^2 - 7} &= \frac{9}{4(\infty)^2 - 7} \\ &= \frac{9}{4\infty - 7} &= \frac{9}{\infty - 7} &= \frac{9}{\infty} \\ &= 0 \end{aligned}$$

Calculus on a Variety of Functions ... (set 3)

Continuity and Differentiability

Question 7: Which of the following functions are *NOT* everywhere continuous:

(A) $f(x) = \frac{x^2-4}{x+2}$

(B) $f(x) = (x + 3)^4$

(C) $f(x) = 1066$

(D) $f(x) = mx + b$

(E) None of the above

Calculus on a Variety of Functions ... (set 3)

Continuity and Differentiability

Answer

Question 7: Which of the following functions are *NOT* everywhere continuous:

(A) $f(x) = \frac{x^2-4}{x+2}$

(B) $f(x) = (x+3)^4$

(C) $f(x) = 1066$

(D) $f(x) = mx + b$

(E) None of the above

Answer: (A) Remember that, informally at least, a *continuous* function is one in which there are no breaks its curve. A continuous function can be drawn without lifting your pencil from the paper. More formally, a function $f(x)$ is *continuous* at the point $x = a$ if and only if:

1. $f(x)$ is defined at the point $x = a$,
2. the limit $\lim_{x \rightarrow a} f(x)$ exists,
3. $\lim_{x \rightarrow a} f(x) = f(a)$

The function $f(x) = \frac{x^2-4}{x+2}$ is not everywhere continuous because the function is not defined at the point $x = -2$. It is worth noting that $\lim_{x \rightarrow -2} f(x)$ does in fact exist! The existence of a limit at a point does not guarantee that the function is continuous at that point!

Calculus on a Variety of Functions ... (set 3)

Continuity and Differentiability

Question 8: Which of the following functions are continuous:

(A) $f(x) = |x|$

(B) $f(x) = \begin{cases} 3 & x < 4 \\ \frac{1}{2}x + 3 & x \geq 4 \end{cases}$

(C) $f(x) = \frac{1}{x}$

(D) $f(x) = \begin{cases} \ln x & x < 0 \\ 0 & x = 0 \end{cases}$

(E) None of the above

Calculus on a Variety of Functions ... (set 3)

Continuity and Differentiability

Answer

Question 8: Which of the following functions are continuous:

(A) $f(x) = |x|$

(B) $f(x) = \begin{cases} 3 & x < 4 \\ \frac{1}{2}x + 3 & x \geq 4 \end{cases}$

(C) $f(x) = \frac{1}{x}$

(D) $f(x) = \begin{cases} \ln x & x < 0 \\ 0 & x = 0 \end{cases}$

(E) None of the above

Answer: (A) The absolute value function $f(x) = |x|$ is defined as:

$$f(x) = \begin{cases} x & x \geq 0 \\ -x & x < 0 \end{cases}$$

Does this function satisfy the requirements for continuity? Yes! The critical point to check is $x = 0$. Note that the function is defined at $x = 0$; the $\lim_{x \rightarrow 0} f(x)$ exists; and that $\lim_{x \rightarrow 0} f(x) = 0 = f(0)$.

Calculus on a Variety of Functions ... (set 3)

Continuity and Differentiability

Question 9: Which of the following functions are *NOT* differentiable:

(A) $f(x) = |x|$

(B) $f(x) = (x + 3)^4$

(C) $f(x) = 1066$

(D) $f(x) = mx + b$

(E) None of the above

Calculus on a Variety of Functions ... (set 3)

Continuity and Differentiability

Answer

Question 9: Which of the following functions are *NOT* differentiable:

(A) $f(x) = |x|$

(B) $f(x) = (x + 3)^4$

(C) $f(x) = 1066$

(D) $f(x) = mx + b$

(E) None of the above

Answer: (A) Remember that continuity is a *necessary* condition for differentiability (i.e., every differentiable function is continuous), but continuity is not a *sufficient* condition to ensure differentiability (i.e., not every continuous function is differentiable). Case in point is $f(x) = |x|$. This function is in fact continuous (see previous question). It is not however differentiable at the point $x = 0$. Why? The point $x = 0$ is a cusp (or kink). There are an infinite number of lines that could be tangent to the function $f(x) = |x|$ at the point $x = 0$, and thus the derivative of $f(x)$ would have an infinite number of possible values.

Calculus on a Variety of Functions ... (set 3)

Derivatives

Question 10: Find the derivative of the following function:

$$f(x) = 1963$$

- (A) $+\infty$
- (B) 1963
- (C) $-\infty$
- (D) 0
- (E) None of the above

Calculus on a Variety of Functions ... (set 3)

Derivatives

Answer

Question 10: Find the derivative of the following function:

$$f(x) = 1963$$

- (A) $+\infty$
- (B) 1963
- (C) $-\infty$
- (D) 0
- (E) None of the above

Answer: (D) The derivative of a constant function is always zero.

Calculus on a Variety of Functions ... (set 3)

Derivatives

Question 11: Find the derivative of the following function:

$$f(x) = x^2 + 6x + 9$$

- (A) $f'(x) = 2x + 6 + 9$
- (B) $f'(x) = x^2 + 6$
- (C) $f'(x) = 2x + 6$
- (D) $f'(x) = 2x$
- (E) None of the above

Calculus on a Variety of Functions ... (set 3)

Derivatives

Answer

Question 11: Find the derivative of the following function:

$$f(x) = x^2 + 6x + 9$$

- (A) $f'(x) = 2x + 6 + 9$
- (B) $f'(x) = x^2 + 6$
- (C) $f'(x) = 2x + 6$
- (D) $f'(x) = 2x$
- (E) None of the above

Answer: (C) Remember that 1) the derivative of a sum of functions is simply the sum of the derivatives of each of the functions, and 2) the power rule for derivatives says that if $f(x) = kx^n$, then $f'(x) = nkx^{n-1}$. Thus $f'(x) = 2x^{2-1} + 6x^{1-1} + 0 = 2x + 6$.

Calculus on a Variety of Functions ... (set 3)

Derivatives

Question 12: Find the derivative of the following function:

$$f(x) = x^{\frac{1}{2}}$$

- (A) $f'(x) = -\frac{1}{2\sqrt{x}}$
- (B) $f'(x) = \frac{1}{\sqrt{x}}$
- (C) $f'(x) = \frac{1}{2\sqrt{x}}$
- (D) $f'(x) = \sqrt{x}$
- (E) None of the above

Calculus on a Variety of Functions ... (set 3)

Derivatives

Answer

Question 12: Find the derivative of the following function:

$$f(x) = x^{\frac{1}{2}}$$

(A) $f'(x) = -\frac{1}{2\sqrt{x}}$

(B) $f'(x) = \frac{1}{\sqrt{x}}$

(C) $f'(x) = \frac{1}{2\sqrt{x}}$

(D) $f'(x) = \sqrt{x}$

(E) None of the above

Answer: (C) Remember that the power rule for derivatives works with fractional exponents as well! Thus $f'(x) = \frac{1}{2}x^{\frac{1}{2}-1} = \frac{1}{2}x^{-\frac{1}{2}} = \frac{1}{2\sqrt{x}}$.

Calculus on a Variety of Functions ... (set 3)

Derivatives

Question 13: Find the derivative of the following function:

$$f(x) = 5x^2(x + 47)$$

- (A) $f'(x) = 15x^2 + 470x$
- (B) $f'(x) = 5x^2 + 470x$
- (C) $f'(x) = 10x$
- (D) $f'(x) = 15x^2 - 470x$
- (E) None of the above

Calculus on a Variety of Functions ... (set 3)

Derivatives

Answer

Question 13: Find the derivative of the following function:

$$f(x) = 5x^2(x + 47)$$

- (A) $f'(x) = 15x^2 + 470x$
- (B) $f'(x) = 5x^2 + 470x$
- (C) $f'(x) = 10x$
- (D) $f'(x) = 15x^2 - 470x$
- (E) None of the above

Answer: (A) Ideally, you would solve this problem by applying the product rule. Set $g(x) = 5x^2$ and $h(x) = (x + 47)$, then $f(x) = g(x)h(x)$. Apply the product rule:

$$\begin{aligned} f'(x) &= g'(x)h(x) + g(x)h'(x) \\ &= 10x(x + 47) + 5x^2(1) \\ &= 10x^2 + 470x + 5x^2 \\ &= 15x^2 + 470x \end{aligned}$$

Calculus on a Variety of Functions ... (set 3)

Derivatives

Question 14: Find the derivative of the following function:

$$f(x) = \frac{5x^2}{x + 47}$$

(A) $f'(x) = \frac{5x^2 - 470x}{(x + 47)^2}$

(B) $f'(x) = \frac{10x^2 + 470x}{(x + 47)^2}$

(C) $f'(x) = 10x$

(D) $f'(x) = \frac{5x^2 + 470}{(x + 47)^2}$

(E) None of the above

Calculus on a Variety of Functions ... (set 3)

Derivatives

Answer

Question 14: Find the derivative of the following function:

$$f(x) = \frac{5x^2}{x+47}$$

(A) $f'(x) = \frac{5x^2-470x}{(x+47)^2}$

(B) $f'(x) = \frac{10x^2+470x}{(x+47)}$

(C) $f'(x) = 10x$

(D) $f'(x) = \frac{5x^2+470}{(x+47)^2}$

(E) None of the above

Answer: (E) Ideally, you would solve this problem by applying the quotient rule. Set $g(x) = 5x^2$ and $h(x) = (x+47)$, then $f(x) = \frac{g(x)}{h(x)}$. Apply the quotient rule:

$$\begin{aligned} f'(x) &= \frac{g'(x)h(x) - g(x)h'(x)}{h(x)^2} \\ &= \frac{10x(x+47) - 5x^2(1)}{(x+47)^2} \\ &= \frac{10x^2 + 470x - 5x^2}{(x+47)^2} \\ &= \frac{5x^2 + 470x}{(x+47)^2} \end{aligned}$$

Calculus on a Variety of Functions ... (set 3)

Derivatives

Question 15: Find the derivative of the following function:

$$f(x) = 5(x + 47)^2$$

- (A) $f'(x) = 15x^2 + 470x$
- (B) $f'(x) = 10x - 470$
- (C) $f'(x) = 10x + 470$
- (D) $f'(x) = 15x^2 - 470x$
- (E) None of the above

Calculus on a Variety of Functions ... (set 3)

Derivatives

Answer

Question 15: Find the derivative of the following function:

$$f(x) = 5(x + 47)^2$$

(A) $f'(x) = 15x^2 + 470x$

(B) $f'(x) = 10x - 470$

(C) $f'(x) = 10x + 470$

(D) $f'(x) = 15x^2 - 470x$

(E) None of the above

Answer: (C) Ideally, you would solve this problem by applying the chain rule. Set $g(h) = 5h^2$ and $h(x) = (x+47)$, then $f(x) = g(h(x))$. Apply the chain rule:

$$\begin{aligned} f'(x) &= g'(h)h'(x) \\ &= 10h \\ &= 10(x + 47) \\ &= 10x + 470 \end{aligned}$$

Calculus on a Variety of Functions ... (set 3)

Derivatives

Question 16: Find the derivative of the following function:

$$f(x) = (7x - 4)(3x + 8)^4$$

Calculus on a Variety of Functions ... (set 3)

Derivatives

Answer

Question 16: Find the derivative of the following function:

$$f(x) = (7x - 4)(3x + 8)^4$$

Answer: Combine the product rule and the chain rule:

$$\begin{aligned} f'(x) &= 7(3x + 8)^4 + (7x - 4)(4)(3)(3x + 8)^3 \\ &= 7(3x + 8)^4 + 12(7x - 4)(3x + 8)^3 \\ &= 7(3x + 8)^4 + (84x - 48)(3x + 8)^3 \end{aligned}$$

Calculus on a Variety of Functions ... (set 3)

Derivatives

Question 17: Find the derivative of the following function:

$$f(x) = (122x^3 - 49)^{-4}$$

Calculus on a Variety of Functions ... (set 3)

Derivatives

Answer

Question 17: Find the derivative of the following function:

$$f(x) = (122x^3 - 49)^{-4}$$

Answer: Use the chain rule:

$$\begin{aligned} f'(x) &= -4 * (122)(3)x^2(122x^3 - 49)^{-5} \\ &= -\frac{1464x^2}{(122x^3 - 49)^5} \end{aligned}$$

Calculus on a Variety of Functions ... (set 3)

Derivatives

Question 18: Find the derivative of the following function:

$$f(x) = \frac{8x^2 + 3x - 9}{7x^2 - 4}$$

Calculus on a Variety of Functions ... (set 3)

Derivatives

Answer

Question 18: Find the derivative of the following function:

$$f(x) = \frac{8x^2 + 3x - 9}{7x^2 - 4}$$

Answer: The easiest way is to solve this is to get rid of the fraction, and then combine the product rule with the chain rule:

$$\begin{aligned} f(x) &= (8x^2 + 3x - 9)(7x^2 - 4)^{-1} \\ f'(x) &= (8(2)x + 3)(7x^2 - 4)^{-1} + (8x^2 + 3x - 9)(-1)(7x^2 - 4)^{-2} \\ &= \frac{16x + 3}{7x^2 - 4} - \frac{8x^2 + 3x - 9}{(7x^2 - 4)^2} \end{aligned}$$

Calculus on a Variety of Functions ... (set 3)

Derivatives

Question 19: Find the derivative of the following function:

$$f(x) = (22 - 9x^6)^{\frac{1}{2}}$$

Calculus on a Variety of Functions ... (set 3)

Derivatives

Answer

Question 19: Find the derivative of the following function:

$$f(x) = (22 - 9x^6)^{\frac{1}{2}}$$

Answer: Use the chain rule:

$$\begin{aligned} f'(x) &= \frac{1}{2}(22 - 9x^6)^{-\frac{1}{2}}(9)(6)x^5 \\ &= 7(3x + 8)^4 + 12(7x - 4)(3x + 8)^3 \\ &= \frac{27x^5}{2(22 - 9x^6)^{\frac{1}{2}}} \end{aligned}$$

Calculus on a Variety of Functions ... (set 3)

Derivatives

Question 20: Find the derivative of the following function:

$$f(x) = (18x^2 + 23)^{\frac{1}{3}}$$

Calculus on a Variety of Functions ... (set 3)

Derivatives

Answer

Question 20: Find the derivative of the following function:

$$f(x) = (18x^2 + 23)^{\frac{1}{3}}$$

Answer: Use the chain rule:

$$\begin{aligned} f'(x) &= \frac{1}{3}(2)(18)x(18x^2 + 23)^{-\frac{1}{3}} \\ &= \frac{12x}{(18x^2 + 23)^{\frac{1}{3}}} \end{aligned}$$

Calculus on a Variety of Functions ... (set 3)

Derivatives

Question 21: Find the derivative of the following function:

$$f(x) = 5x^2(4x - 9)^3$$

Calculus on a Variety of Functions ... (set 3)

Derivatives

Answer

Question 21: Find the derivative of the following function:

$$f(x) = 5x^2(4x - 9)^3$$

Answer: Combine the product rule and the chain rule:

$$\begin{aligned} f'(x) &= 5(2)x(4x - 9)^3 + 5x^2(3)(4)(4x - 9)^2 \\ &= 10x(4x - 9)^3 + 60x^2(4x - 9)^2 \end{aligned}$$

Calculus on a Variety of Functions ... (set 3)

Higher Order Derivatives

Question 22: Find the second derivative of the following function:

$$f(x) = 5x^2(x + 47)$$

- (A) $f''(x) = 30x - 470$
- (B) $f''(x) = 30x + 470$
- (C) $f''(x) = 15x^2 + 235$
- (D) $f''(x) = 15x^2 + 470x$
- (E) None of the above

Calculus on a Variety of Functions ... (set 3)

Higher Order Derivatives

Answer

Question 22: Find the second derivative of the following function:

$$f(x) = 5x^2(x + 47)$$

- (A) $f''(x) = 30x - 470$
- (B) $f''(x) = 30x + 470$
- (C) $f''(x) = 15x^2 + 235$
- (D) $f''(x) = 15x^2 + 470x$
- (E) None of the above

Answer: (B) The second derivative is just the derivative of the first derivative. Simplest solution would be to multiply to re-write the function as $f(x) = 5x^2(x+47) = 5x^3+235x^2$. Now take the derivative: $f'(x) = 15x^2+470x$. Taking the derivative again yields the second derivative: $f''(x) = 30x + 470$.

Calculus on a Variety of Functions ... (set 3)

Higher Order Derivatives

Question 23: Find the third derivative of the following function:

$$f(x) = 5x^2(x + 47)$$

- (A) 15
- (B) $15 + x$
- (C) $30x$
- (D) $30x + 470$
- (E) None of the above

Calculus on a Variety of Functions ... (set 3)

Higher Order Derivatives

Answer

Question 23: Find the third derivative of the following function:

$$f(x) = 5x^2(x + 47)$$

- (A) 15
- (B) $15 + x$
- (C) $30x$
- (D) $30x + 470$
- (E) None of the above

Answer: (E) Just take the derivative of your answer to Question 12 to get the third derivative of $f(x) = 5x^2(x + 47)$. Answer: $f'''(x) = 30$.

Calculus on a Variety of Functions ... (set 3)

Higher Order Derivatives

Question 24: Suppose that you have the following utility function:

$$u(x) = \sqrt{x}$$

Find $-\frac{u''(x)}{u'(x)}$.

- (A) $\frac{1}{2x}$
- (B) $-\frac{1}{2x}$
- (C) $2x$
- (D) $-2x$
- (E) None of the above

Calculus on a Variety of Functions ... (set 3)

Higher Order Derivatives

Answer

Question 24: Suppose that you have the following utility function:

$$u(x) = \sqrt{x}$$

Find $-\frac{u''(x)}{u'(x)}$.

- (A) $\frac{1}{2x}$
- (B) $-\frac{1}{2x}$
- (C) $2x$
- (D) $-2x$
- (E) None of the above

Answer: (A) The ratio $-\frac{u''(x)}{u'(x)}$ is called the Arrow-Pratt measure of relative risk aversion and you will encounter it in core microeconomics. The first derivative of the utility function (otherwise known as marginal utility) is $u'(x) = \frac{1}{2\sqrt{x}}$ (see Question 9 above). The second derivative is $u''(x) = -\frac{1}{4}x^{-\frac{3}{2}} = -\frac{1}{4\sqrt{x^3}}$. Thus the Arrow-Pratt measure of relative risk aversion is:

$$-\frac{u''(x)}{u'(x)} = -\frac{-\frac{1}{4\sqrt{x^3}}}{\frac{1}{2\sqrt{x}}} = \frac{2\sqrt{x}}{4\sqrt{x^3}} = \frac{1}{2x}$$

Calculus on a Variety of Functions ... (set 3)

Higher Order Derivatives

Question 25: Find the first, second and third derivatives of the following function:

$$f(x) = 3x^4 - 5x^3 + 8x^2 - 7x - 13$$

Calculus on a Variety of Functions ... (set 3)

Higher Order Derivatives

Answer

Question 25: Find the first, second and third derivatives of the following function:

$$f(x) = 3x^4 - 5x^3 + 8x^2 - 7x - 13$$

Answer:

$$f'(x) = 12x^3 - 15x^2 + 16x - 7$$

$$f''(x) = 36x^2 - 30x + 16$$

$$f'''(x) = 72x - 30$$

Calculus on a Variety of Functions ... (set 3)

Higher Order Derivatives

Question 26: Find the first, second and third derivatives of the following function:

$$f(x) = (5 - 2x)^4$$

Calculus on a Variety of Functions ... (set 3)

Higher Order Derivatives

Answer

Question 26: Find the first, second and third derivatives of the following function:

$$f(x) = (5 - 2x)^4$$

Answer:

$$f'(x) = 4(-2)(5 - 2x)^3 = -8(5 - 2x)^3$$

$$f''(x) = -8(3)(-2)(5 - 2x)^2 = 48(5 - 2x)^2$$

$$f'''(x) = 48(2)(-2)(5 - 2x) = -192(5 - 2x) = 384x - 960$$