Evaluate each limit algebraically. No calculator.

1.
$$\lim_{x\to 0} (3x+5)$$

2.
$$\lim_{x\to 5} (2-3x)$$

3.
$$\lim_{x\to 8} (8-x)$$

$$4. \quad \lim_{x \to 3} \frac{x+2}{x}$$

$$5. \quad \lim_{x \to 0} \frac{x+2}{x}$$

6.
$$\lim_{x \to 4} \frac{x^2 - 16}{x - 4}$$

7.
$$\lim_{x \to 2} \frac{x^3 - 8}{2 - x}$$

8.
$$\lim_{x \to 2} \frac{x^2 + 2x - 8}{x - 2}$$

8.
$$\lim_{x \to 2} \frac{x^2 + 2x - 8}{x - 2}$$
 9. $\lim_{x \to 4} \frac{2x^2 - 5x - 12}{x - 4}$

10.
$$\lim_{x \to -5} \frac{x+5}{x^3 + 125}$$

11.
$$\lim_{x \to 3} \frac{x^3 - 3x^2 - 4x + 12}{x - 3}$$

12.
$$\lim_{x \to 2} \frac{x^3 - 2x^2 + 3x - 6}{x^2 - 4}$$

13.
$$\lim_{x \to 3} \frac{x-3}{\frac{1}{x} - \frac{1}{3}}$$

14.
$$\lim_{x \to 0} \frac{\frac{1}{x+4} - \frac{1}{4}}{x}$$

15.
$$\lim_{x \to 9} \frac{\sqrt{x} - 3}{x - 9}$$

16.
$$\lim_{x \to 0} \frac{x}{\sqrt{x+4}-2}$$

17.
$$\lim_{x \to 1} \frac{x^2 - \sqrt{x}}{x^4 - 1}$$

Evaluate each limit and then identify any horizontal asymptotes.

18.
$$\lim_{x \to \infty} \frac{x^3 + 8x - 4}{2x^3 + 3}$$

19.
$$\lim_{x \to \infty} \frac{x^2 - 1}{2x^3 - 8x^2 + 3}$$
 20. $\lim_{x \to \infty} \frac{x^5 - x - 1}{6x^3}$

20.
$$\lim_{x \to \infty} \frac{x^5 - x - 1}{6x^3}$$

21.
$$\lim_{x \to \infty} \frac{x+1}{x^2 - 1}$$

$$22. \lim_{x \to \infty} \frac{x^2 - 1}{x + 1}$$

Evaluate each limit and then identify any vertical asymptotes.

23.
$$\lim_{x \to 2} \frac{5x^2 + x}{x - 2}$$

24.
$$\lim_{x \to 1} \frac{x}{(x-1)^3}$$

25.
$$\lim_{x \to -3} \frac{x^2 + 2x - 15}{x^2 - 9}$$

Answers

1) 5

6) 8

11) 5

16) 4

21) 0, y = 0

2) -13

7) -12

12) 7/4

17) 3/8

21) und, no HA

3) 0

8) 6

13) -9

23) und, x = 2

4) 5/3

9) 11

18) $\frac{1}{2}$, y = 1/219) 0, y = 0

24) und, x = 1

5) undefined

10) 1/75

15) 1/6

14) -1/16

20) und, no HA

25) und, x = 3