

Right Triangle Trigonometry

Trigonometric Ratios

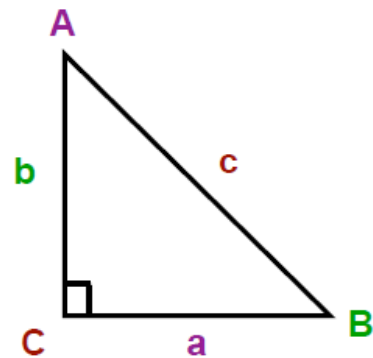
(SOH-CAH-TOA)

Trigonometry - a branch of mathematics that studies the relationships between the sides and angles of triangles.

Trigonometric ratio - the ratio between two sides of a right triangle.

There are 3 "trig ratios" that we will study.
The ratios are called **sine**, **cosine**, and **tangent**.

They are abbreviated **sin**, **cos**, and **tan** respectively (locate these buttons on your calculator).



What do these trig ratios stand for?

$$\sin x = \frac{\text{opposite side}}{\text{hypotenuse}}$$

SOH

$$\cos x = \frac{\text{adjacent side}}{\text{hypotenuse}}$$

CAH

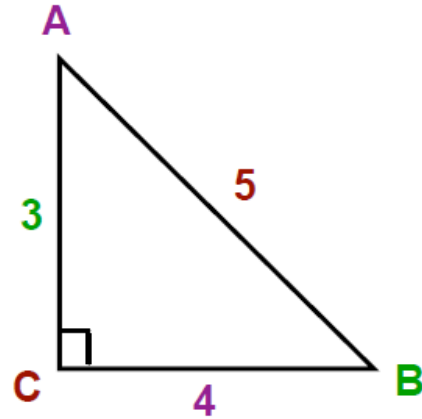
$$\tan x = \frac{\text{opposite side}}{\text{adjacent side}}$$

TOA

The mnemonic device to remember the 3 trig ratios is

"SOH-CAH-TOA"

SOHCAHTOA



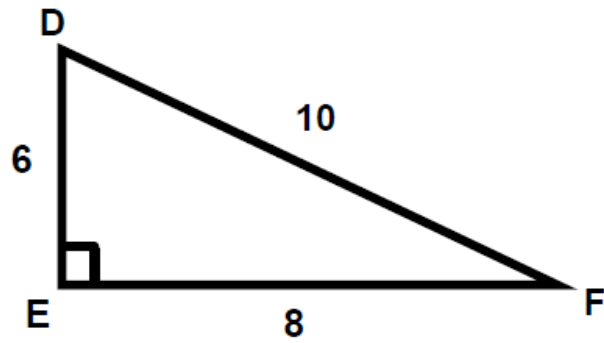
Example 1: Let's look at $\angle A$.

Find the side opposite, side adjacent, and the hypotenuse for $\angle A$.

Then write the $\sin A$, $\cos A$, and $\tan A$ ratios.

SOH-CAH-TOA ... Set 2

Example 2



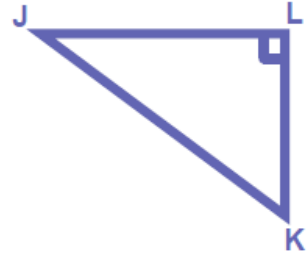
Find $\sin F$, $\cos F$, and $\tan F$.

SOH-CAH-TOA ... Set 2

What is the side opposite of $\angle J$?

What is the hypotenuse of the triangle?

What is the side adjacent to $\angle J$?

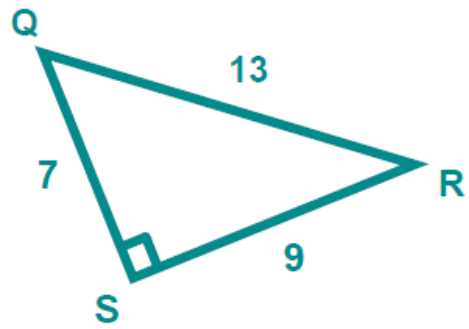


SOH-CAH-TOA ... Set 2

What is $\sin R$?

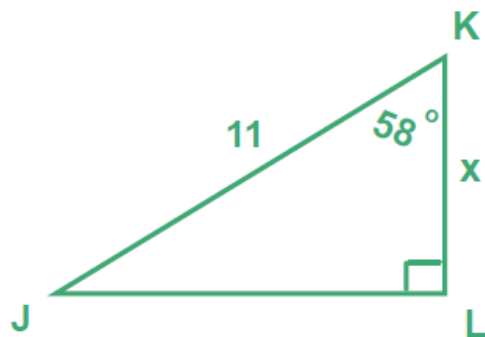
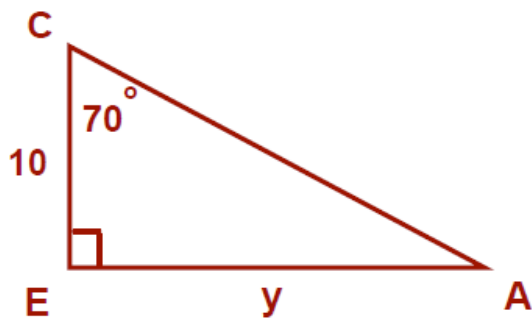
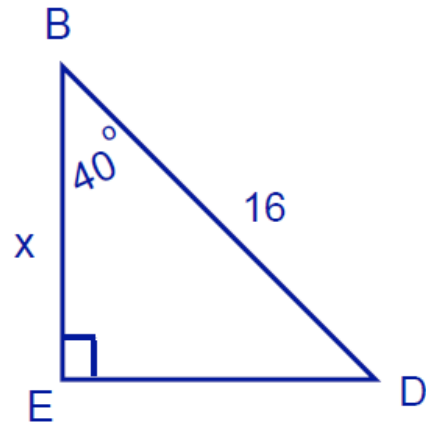
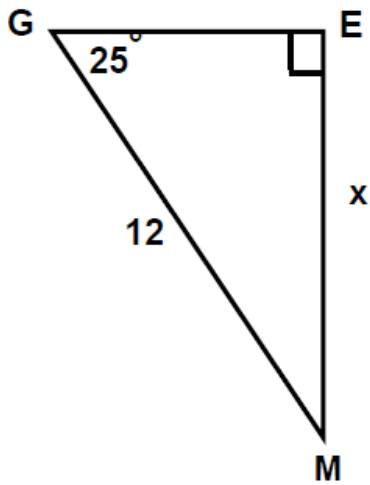
What is $\cos R$?

What is $\tan R$?



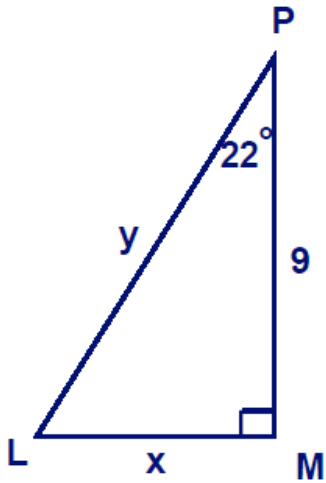
Using Trigonometric Ratios to find side lengths
(You will need a calculator for this)

Solve for the missing side lengths:

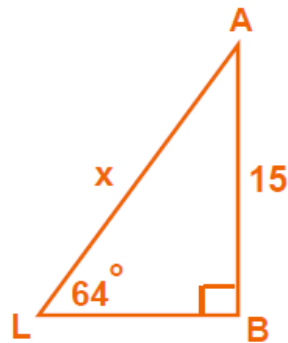
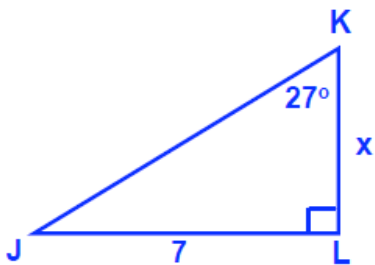
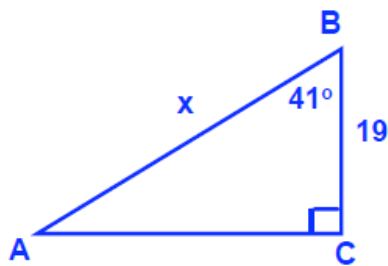
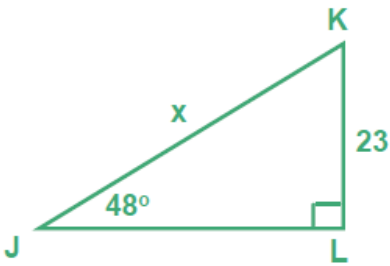


SOH-CAH-TOA ... Set 2

Solve for the missing side lengths:



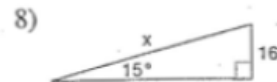
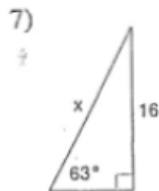
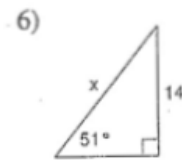
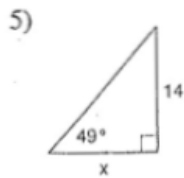
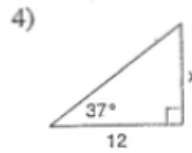
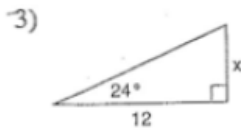
How do we solve if the variable is in the denominator of the fraction?



SOH-CAH-TOA ... Set 2

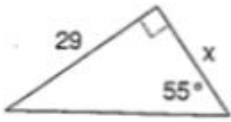
Label each triangle with adjacent, opposite and hypotenuse.

Then decide which formula you would use.

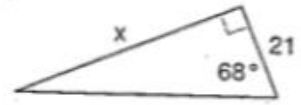


SOH-CAH-TOA ... Set 2

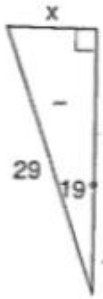
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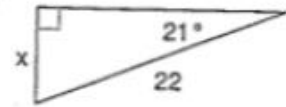
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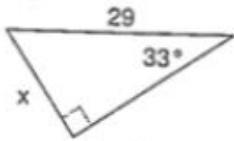
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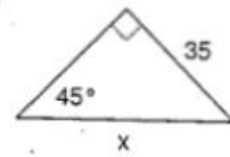
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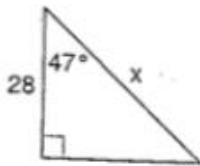
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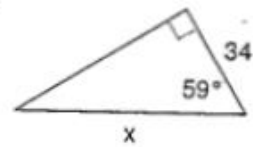
14)



15)



16)



Using Inverse Trigonometric Ratios to find angle measures

(You will need a calculator for this)

In this section you will need to use the **inverse trig functions** to solve for missing angles. Just as the following are inverses and undo each other,

Addition $\xleftrightarrow{\text{inverse}}$ Subtraction
 Multiplication $\xleftrightarrow{\text{inverse}}$ Division
 Square $\xleftrightarrow{\text{inverse}}$ Square Root

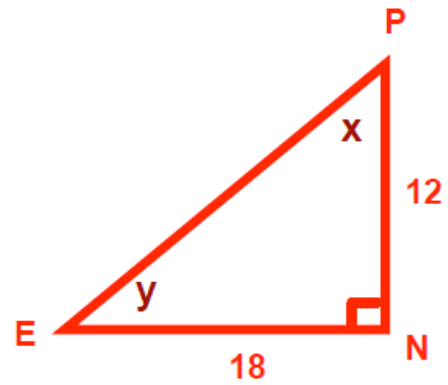
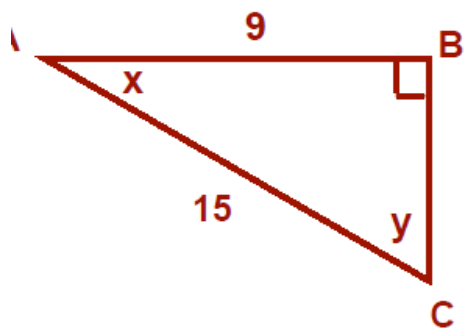
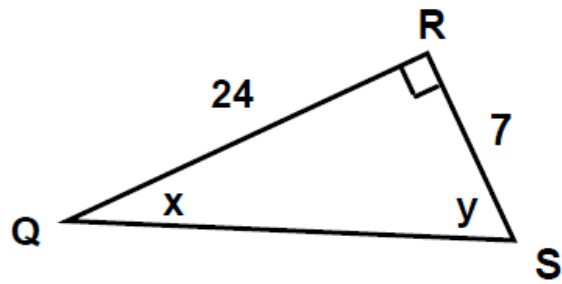
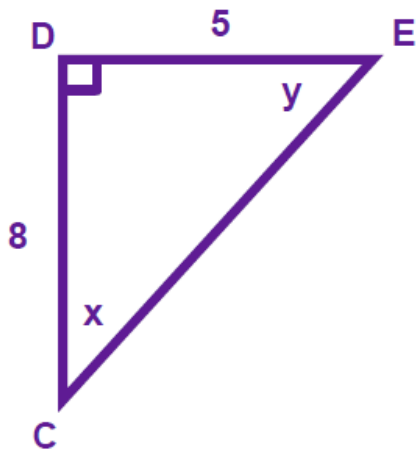
so does a trig ratio and its inverse.

$\sin \theta \xleftrightarrow{\text{inverse}} \sin^{-1} \theta$
 $\cos \theta \xleftrightarrow{\text{inverse}} \cos^{-1} \theta$
 $\tan \theta \xleftrightarrow{\text{inverse}} \tan^{-1} \theta$

"To find the degree, use the inverse key"

SOH-CAH-TOA ... Set 2

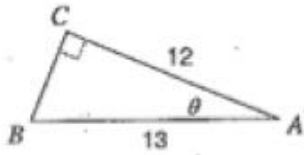
Solve for the missing angle measures:



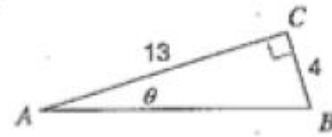
SOH-CAH-TOA ... Set 2

Find the measure of each angle indicated. Round to the nearest tenth.

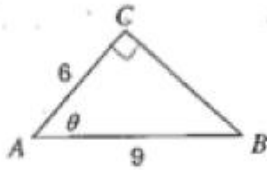
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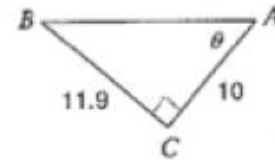
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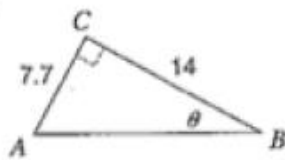
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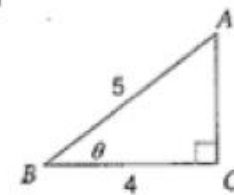
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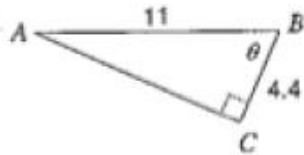
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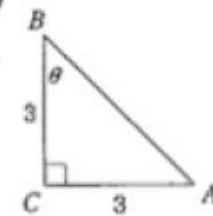
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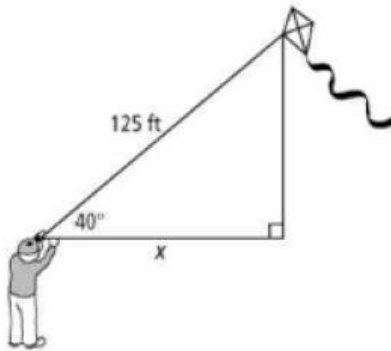
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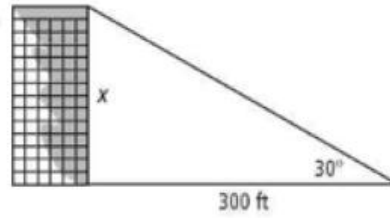
SOH-CAH-TOA ... Set 2

Find the value of x . Round to the nearest tenth of a unit.

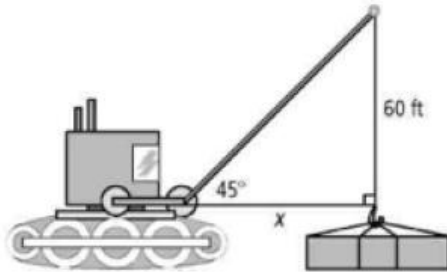
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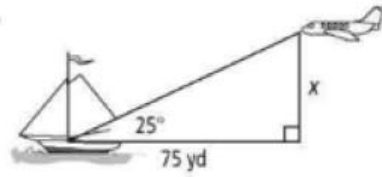
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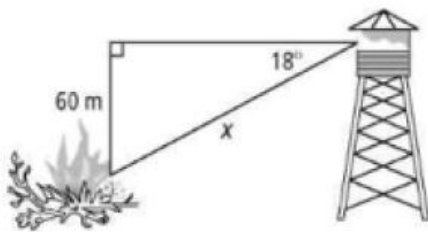


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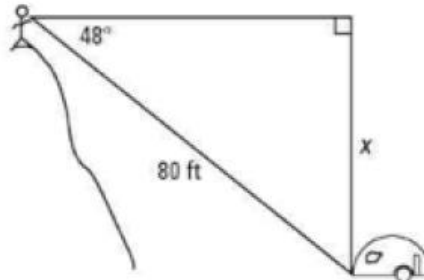


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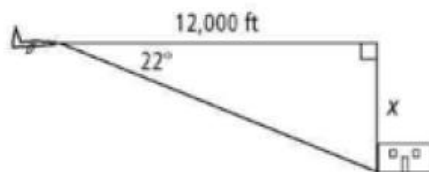
16.



17.



18.



19.

