

## Basic Probability Formulas

Complementary events: The complement of event A is everything not in A. Complementary events are mutually exclusive events and together make up the sample space. The probability of the sample space is one.

Independent events: The occurrence of any one of the events does not affect the probabilities of the occurrences of the other events. Events A and B are independent if probability of A given B equals probability of A.

Dependent events (or non-independent events): Events that are not independent, i.e.,  $P(A \text{ given } B) \neq P(A)$ .

Mutually exclusive events (or disjoint events): If event A occurs, then event B cannot occur, and conversely.

De Morgan's Rule (one form): Via a double complement,  $A \text{ or } B = (A^c \text{ and } B^c)^c = \text{"not [ (not A) and (not B) ]"}$ . For example, "I want A, B, or both to work" (Reliability) equates to "I do not want both A and B not to work" (Safety).

Event	Details	Formula (from English to mathematical operations)
A	Probability of A, $P(A)$	<b>P(A) is at or between zero and one: <math>0 \leq P(A) \leq 1</math></b>
not A, $A^c$	$A^c$ is the complement of A	<b>Probability of not A = <math>P(A^c) = 1 - P(A)</math></b>

Event	Details	Formula (from English to mathematical operations)
A and B	A and B are <b>independent</b> events	$P(A \text{ and } B) = P(A) \cdot P(B)$
	A and B are <b>dependent</b> events	$P(A \text{ and } B) = P(A) \cdot P(B   A) = P(B) \cdot P(A   B)$ as 2 forms
	A and B are <b>mutually exclusive</b> events	$P(A \text{ and } B) = 0$

Event	Details	Formula (from English to mathematical operations)
A or B	A and B are <b>independent</b> events	$P(A \text{ or } B) = P(A) + P(B) - P(A) \cdot P(B)$ conveniently expands to $= 1 - [1 - P(A)] \cdot [1 - P(B)]$ or is obtained from De Morgan's Rule
	A and B are <b>dependent</b> events	$P(A \text{ or } B) = P(A) + P(B) - P(A) \cdot P(B   A)$ as 1 of 2 forms
	A and B are <b>mutually exclusive</b> events	$P(A \text{ or } B) = P(A) + P(B)$